

Week 10: DOE & Power Analysis

m EMSE 6035: Marketing Analytics for Design Decisions

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📩 October 30, 2024

Quiz 4

Link is in the #class channel





Week 10: DOE & Power Analysis

1. Design of Experiment

2. Design Efficiency

3. Power Analysis

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Main & Interaction Effects

Full design space for 3 effects: A, B, C



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Full design space for 3 effects: A, B, C

- Example: Cars A: Electric? (Yes+ or No-) B: Warranty? (Yes+ or No-)
- C: Ford? (Yes+ or No-)



Main Effects



Interaction Effects



Example: Wine Pairings

meat wine

fish white fish red steak white

steak red

Main Effects

meat: Fish or Steak?
 wine: Red or White?

Example: Wine Pairings

meat wine

fish white fish red steak white steak red

Main Effects

meat: Fish or Steak?
 wine: Red or White?

Interaction Effects

meat*wine: Red or White wine with Steak?
 meat*wine: Red or White wine with Fish?

Open interactions.qmd

Fractional vs Full Factorial Designs

Full Factorial Design

Example: Cars

A: Electric? (Yes+ or No-)

B: Warranty? (Yes+ or No-)

C: Ford? (Yes+ or No-)

```
library(cbcTools)
```

```
profiles <- cbc_profiles(
     electric = c(1, 0),
     warranty = c(1, 0),
     ford = c(1, 0)
)</pre>
```

profiles

#>		profileID	electric	warranty	ford	
#>	1	1	1	1	1	
#>	2	2	0	1	1	
#>	3	3	1	0	1	
#>	4	4	0	0	1	
#>	5	5	1	1	0	
#>	6	6	0	1	0	
#>	7	7	1	0	0	
#>	8	8	0	0	0	

Full Factorial Design

Balanced?

All levels appear an equal number of times.

Orthogonal?

All pairs of levels appear together an equal number of times.

library(cbcTools)

```
profiles <- cbc_profiles(
    electric = c(1, 0),
    warranty = c(1, 0),
    ford = c(1, 0)
)</pre>
```

profiles

#>	profileID	electric	warranty	ford
#> 1	1	1	1	1
#> 2	2 2	0	1	1
#> 3	3	1	0	1
#> 4	4	0	0	1
#> 5	5 5	1	1	0
#> 6	5 6	0	1	0
#> 7	7 7	1	0	0
#> 8	8 8	0	0	0

Fractional Factorial Design

Balanced?

All levels appear an equal number of times.

Orthogonal?

All pairs of levels appear together an equal number of times.

profiles[c(1, 3, 5, 6),]

#>		profileID	electric	warranty	ford
#>	1	1	1	1	1
#>	3	3	1	0	1
#>	5	5	1	1	0
#>	6	6	0	1	0

Comparing Full and Fractional Factorial Designs Open balance-orthogonality.qmd

Practice Question 1

Consider the following experiment design

а	b	С	Effect
+	-	-	А
	+		В
÷	-	+	AC
-	+	+	BC

a) Is the design balanced? Is is orthogonal?

b) Write out the equation to compute the main effect for a, b, and c.

c) Are any main effects confounded? If so, what are they confounded with?

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A simple conjoint experiment about cars

Attribute	Levels
Brand	GM, BMW, Ferrari
Price	\$20k, \$40k, \$100k

Design: 9 choice sets, 3 alternatives each

Attribute counts:	Pairwis
brand: GM BMW Ferrari 10 11 6	brand &
price:	GM BMW
20k 40k 100k 9 9 9	гегта

Pairwise a	Pairwise attribute counts:				
brand & pr	rice:				
	20k	40k	100k		
GM	3	0	7		
BMW	4	5	2		
Ferrari	2	4	0		

A simple conjoint experiment about cars

Attribute	Levels
Brand	GM, BMW, Ferrari
Price	\$20k, \$40k, \$100k

Design: 90 choice sets, 3 alternatives each

Attribute counts:	Pairwise attribute counts:		
brand: GM BMW Ferrari	brand & price:		
92 80 98	20k 40k 100k GM 31 31 30		
price:	BMW 25 25 30 Ferrari 35 28 35		
20k 40k 100k 91 84 95			

Bayesian D-efficient designs

Maximize information on "Main Effects" according to priors

Attribute	Levels	Prior
Brand	GM, BMW, Ferrari	0, 1, 2
Price	\$20k, \$40k, \$100k	0, -1, -4

$$v_j = 1 \delta^{ ext{BMW}} + 2 \delta^{ ext{Ferrari}} - 1 \delta^{40 ext{k}} - 4 \delta^{100 ext{k}}$$

Bayesian D-efficient designs

Maximize information on "Main Effects" according to priors

Attribute	Levels	Prior
Brand	GM, BMW, Ferrari	0, 1, 2
Price	\$20k, \$40k, \$100k	0, -1, -4

Attribu	Attribute counts:			
brand: GM 93	BMW 90	Ferrari 86		
price:				
20k 97	40k 1 93	00k 78		

Pairwise attribute counts:			
brand & price:			
	201	101	1001
	ZUK	40K	TOOK
GM	52	41	0
BMW	30	30	30
	1 Г	22	40
Ferrari	15	22	49

Negative of the hessian evaluated at a set of parameters is called the "Information Matrix"

$$oldsymbol{I}(oldsymbol{eta}) = -
abla_{oldsymbol{eta}}^2\ln(\mathcal{L})$$

"D-optimal" designs attempt to minimize the "D-error" of a design

$$D = \left| oldsymbol{I}(oldsymbol{eta})
ight|^{-1/p}$$

where p is the number of coefficients in the model

Finding Efficient Designs Open design-efficiency.qmd

Your Turn



- 1. Individually, create a Bayesian D-efficient fractional factorial survey design. Inspect the attribute balance and overlap.
- 2. Compare your results with your teammates.

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How many respondents do I need?

How many respondents do I need to get X level of precision on β ?

Standard errors are inversely related to \sqrt{N}

n <- seq(100)
se <- 1/sqrt(n)
plot(n, se, type = "l")</pre>

Standard errors also decrease with:

- Fewer attributes
- Fewer levels in each categorical attribute
- More questions per respondent



Using {cbcTools}, we can run simulations to determine the necessary sample size for a specific model

Open powerAnalysis.qmd

Your Turn



Individually:

- 1. Using the survey design you created in the last practice, conduct a power analysis to determine the necessary sample size to achieve a 0.05 significance level on your parameter estimates.
- 2. Compare your results with your teammates.